Time Series Lab 4

May 14, 2012

1. A Random Coefficient Regression. Consider the following model,

$$y_t = x_t \beta_t + e_t$$

$$\beta_t = \beta_{t-1} + v_t,$$

where y_t and x_t are year-to-year changes of CPI and PPI, respectively, and $e_t \sim N(0, R)$ and $v_t \sim N(0, Q)$. The data file is cpippi.txt, which can be downloaded from the course webpage. The first column of the file gives the y2y change of CPI, and the second column gives that of PPI.

- (1) Estimate R and Q using MLE.
- (2) Estimate β_t using all information in $(y_t, x_t)_{t=1}^n$.

2. (optional) Markov Switching. Let (r_t) be monthly returns on Shanghai Stock Composite Index since 2000, and consider the following model,

$$\begin{aligned} r_t &= \mu_{s_t} + w_t, \quad s_t \in \{1, 2\} \\ w_t &= \alpha w_{t-1} + \varepsilon_t, \end{aligned}$$

where $\varepsilon_t \sim i.i.d.N(0, \sigma^2)$ and s_t is a Markov chain with transition matrix $\begin{pmatrix} p & 1-p \\ 1-q & q \end{pmatrix}$.

- (1) Estimate all parameters in the model using MLE.
- (2) Calculate and plot $p(s_t | \mathcal{F}_n)$.